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SIDDHARTH INSTITUTE OF ENGINEERING & TECHNOLOGY:: PUTTUR
(AUTONOMOUS)

B.Tech I Year I Semester Supplementary Examinations August-2021

ALGEBRA AND CALCULUS

(Common to all)

Time: 3 hours

Max. Marks: 60

(Answer all Five Units 5 x 12 = 60 Marks)

UNIT-I

1 a Reduce the matrix $A = \begin{bmatrix} 1 & 2 & 3 & 2 \\ 2 & 3 & 5 & 1 \\ 1 & 3 & 4 & 5 \end{bmatrix}$ into Echelon form and find its rank? 6M

b Solve the system of equations $x+2y+3z=0, 3x+4y+4z=0, 7x+10y+12z=0$ 6M

OR

2 Show that the matrix $A = \begin{bmatrix} 1 & -2 & 2 \\ 1 & 2 & 3 \\ 0 & -1 & 2 \end{bmatrix}$ satisfies its characteristic equation and find A^{-1} ? 12M

UNIT-II

3 a Verify Rolle's Theorem for the function $f(x) = \frac{\sin x}{e^x}$ in $(0, \pi)$ 6M

b Verify Cauchy's mean value theorem for the function $\sin x$ and $\cos x$ in $[0, \frac{\pi}{2}]$. 6M

OR

4 Obtain the Maclaurin's series expression of the following functions: 12M
i) e^x ii) $\cos x$ iii) $\sin x$

UNIT-III

5 a If $u = \tan^{-1} \left[\frac{2xy}{x^2 - y^2} \right]$, prove that $\frac{\partial^2 u}{\partial x^2} + \frac{\partial^2 u}{\partial y^2} = 0$ 6M

b If $u = \frac{x+y}{1-xy}$ and $v = \tan^{-1} x + \tan^{-1} y$, find $\frac{\partial(u,v)}{\partial(x,y)}$? 6M

OR

6 Examine the function for extreme values $f(x, y) = x^4 + y^4 - 2x^2 + 4xy - 2y^2$; $(x > 0, y > 0)$. 12M

UNIT-IV

7 a Evaluate the following improper integrals i) $\int_1^{\infty} \frac{1}{x^4} dx$ ii) $\int_0^1 \frac{1}{\sqrt{x}} dx$. 6M

b Evaluate $\int_{-10}^1 \int_{x-z}^{x+z} \int_{x-z}^{x+z} (x+y+z) dx dy dz$ 6M

OR

- 8 Evaluate $\int_0^a \int_{\frac{x}{a}}^{\sqrt{x}} (x^2 + y^2) dy dx$, by changing the order of integration 12M

UNIT-V

- 9 a Define Beta and Gamma functions and Prove that $\Gamma(1) = 1$ 6M
 b Evaluate $\int_0^1 x^4 \left(\log \frac{1}{x}\right)^3 dx$. 6M

OR

- 10 a Prove that $\int_0^{\frac{\pi}{2}} \sin^2 \theta \cos^4 \theta d\theta = \frac{\pi}{32}$ 6M
 b Prove that $\int_0^1 \frac{x}{\sqrt{1-x^5}} dx = \frac{1}{5} B\left(\frac{2}{5}, \frac{1}{2}\right)$. 6M

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